

Interactive Display of Global Illumination Solutions for Non-Diffuse Environments – A Survey

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Abstract

In recent years there has been a lot of work on interactively displaying global illumination solutions for non-diffuse environments. This is an extremely active field of research, in which a lot of different approaches have been proposed recently. In this survey, we will discuss and compare these. This will hopefully lay the ground for systematically addressing the open questions in the future.

1. Introduction

Indirect illumination is an important visual effect that contributes significantly to the realism of computer generated imagery. Thus, it is not surprising that several methods for including these effects in interactive applications have been developed over the past few years.

For example, a common technique for displaying the indirect illumination in a diffuse environment is to use Gouraud shading and texture mapping for displaying the results of a Radiosity simulation^{1, 2, 3, 4}. Due to the view-independent nature of illumination in a diffuse environment, the expensive precomputation step can easily be separated from the inexpensive display step, which allows for high frame rates using graphics hardware.

The case of non-diffuse reflection is more challenging and interesting, because it requires either precomputing and storing a large amount of data, or the execution of relatively expensive operations on the fly. The purpose of this survey is to show the current status quo of methods related to interactive display of global illumination solutions, and to compare the different approaches to each other.

In practice, we find that the different approaches constitute a smooth transition from precomputed illumination with large storage requirements to on-the-fly computations con-

suming little or no memory. For the purposes of this survey, we have grouped the different methods in the following categories:

- Image-based methods using precomputed environment maps (Section 2). These methods ignore parallax effects due to objects that are large compared to their environment. Environment maps allow for an efficient reconstruction based on texture mapping.
- Image-based methods using precomputed light fields (Section 3). As in the case of environment maps, this allows for efficient reconstruction that is mostly a simple table lookup or a lookup combined with some interpolation.
- Reconstruction from sparse or scattered light field information (Section 4). Like the methods in Section 3, these techniques also work on precomputed light fields, but they usually use fairly sparse representations that require a significant amount of work to be performed on the fly during a reconstruction phase.
- On-the-fly methods (Section 5). Here, the global illumination is completely computed during rendering time. This means that dynamic scenes can trivially be handled, but on the other hand the complexity of the scene or the illumination effects that can be dealt with are often seriously limited for performance reasons.

2. Environment Maps

In this part of the tutorial we are going to discuss environment maps⁵ and their applications to interactive rendering. Environment maps are special textures that describe for all directions the incoming or outgoing light at one point in space. The main use of these maps is to simulate mirror reflections in curved objects, but they can be used for a variety of purposes, including the rendering of global illumination solutions with more complex reflection models as described below. Hardware-accelerated renderers, in particular, often use environment maps to store precomputed directional information that is too expensive to compute on the fly.

The basic idea of environment maps is that, if a reflecting object is small compared to its distance from the environment, the incoming illumination on the surface really only depends on the direction of the reflected ray. Its origin, that is the actual position on the surface, can be neglected. Therefore, the incoming illumination at the object can be precomputed and stored in a 2-dimensional texture map.

If the parameterization for this texture map is cleverly chosen, the illumination for reflections off the surface can be looked up very efficiently. Of course, the assumption of a small object compared to the environment often does not hold, but environment maps are a good compromise between rendering quality and the need to store the full 4-dimensional radiance field on the surface.

Both offline⁶ and interactive, hardware-based renderers⁷ have used this approach to simulate mirror reflections, often with amazing results.

In this section, we first discuss the issue of parameterizations (or representations) for environment mapping. Afterwards, we compare techniques for using environment maps for matte reflections and different reflection models.

2.1. Parameterizations for Environment Maps

Since environment maps represent directional information as a 2D texture, it is necessary to decide for a mapping from directions to texture coordinates in order to define a concrete representation. This mapping, called the *parameterization* of the environment map, should fulfill a couple of properties in order to be useful for interactive rendering:

- for walkthroughs of static environments, it should not be necessary to create a new environment map every frame. This means that
 - the computation of the texture coordinates is possible for all viewing directions.
 - all light directions need to be represented equally well in the environment map. Although some light directions are more important than others for a certain viewing direction, all directions are equally important for a walkthrough, where the viewing direction is not previ-

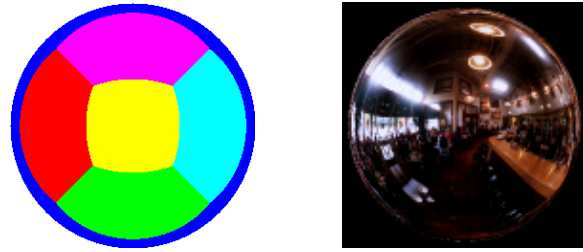


Figure 1: Left: A spherical environment map from the center of a colored cube. Note the bad sampling of the cube face directly in front of the observer (black). Right: a spherical map of a real scene.

ously known. This property is called the *uniformity* of the parameterization.

- for interaction with dynamic environments, it should be easy and inexpensive to create a new environment map from perspective images of the scene (because this is what current hardware can generate).
- the method for computing the texture coordinates should be simple and efficient, and it should be easy to implement in hardware. This means that complicated and expensive mathematical functions like trigonometric functions should not be necessary.

In the following, we briefly discuss the three parameterizations for environment maps that have gained some importance in interactive and hardware-accelerated rendering.

Spherical Maps. The parameterization traditionally used in computer graphics hardware is the *spherical environment map*⁸. It is based on the analogy of a small, perfectly mirroring metal ball centered around the object. The image that an orthographic camera sees when looking at such a ball from a certain viewing direction is the environment map. An example environment map from the center of a colored cube is shown on the left of Figure 1, a map of a real scene is shown on the right.

The sampling rate of spherical maps reaches its maximum for directions opposing the viewing direction (that is, objects behind the viewer), and goes towards zero for directions close to the viewing direction, because these correspond to the tangential areas of the virtual metal ball used to generate the map. Because of this singularity in the viewing direction, it is clear that this parameterization is not suitable for viewing directions other than the original one, especially since the automatic texture coordinate mode does not support this case. Thus, maps using this parameterization have to be regenerated for each change of the view point, even if the environment is otherwise static. The creation of a spherical map requires a texture mapping step in which perspective images are warped into the spherical form.

Despite these disadvantages, the spherical map is very

useful if the only interaction with the scene is rotating an object in front of the screen. This is the case, for example, in design and CAD applications.

Cube Maps. The second parameterization, *cubical environment maps* or *cube maps*^{9, 10} consist of six independent perspective images from the center of a cube through each of its faces. From this description it is clear that the generation of such a map simply consists of rendering the six perspective images. A warping step as required for spherical maps is not necessary. The sampling of these maps is fairly good. It can be shown that the sampling rates for all directions differ by a factor of $3\sqrt{3} \approx 5.2$.

Obviously, this parameterization is suitable for arbitrary viewing directions, and several current PC graphics boards support it via a specific OpenGL extension. One problem here is the use of six independent textures, which requires some special mechanisms in the texture specification. Also, the separation into six textures may produce seams between the cube faces. In particular, this is the case if mip-mapping is used, because then each face is downsampled individually. It would be possible to overcome these problems by adding a border of several pixels to each of the faces, and to replicate some information from neighboring faces there.

Parabolic Maps. Finally, *Parabolic maps*^{11, 12}, sometimes also called *dual paraboloid maps*, are based on an analogy similar to the one used to describe spherical environment maps. Assume that the reflecting object lies at the origin, and that the viewing direction is along the negative z axis. The image seen by an orthographic camera when looking at a metallic, reflecting paraboloid contains the information about the hemisphere facing towards the viewer. The complete environment is stored in two separate textures, each containing the information of one hemisphere. The geometry is depicted in Figure 2.

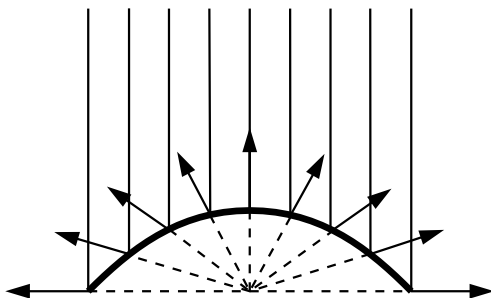


Figure 2: The rays of an orthographic camera reflected off a paraboloid sample a complete hemisphere of directions.

The geometry described above has some interesting properties. Firstly, the reflected rays in each point of the paraboloid all originate from a single point, the focal point of the paraboloid, which is also the origin of the coordinate system (see dashed lines in Figure 2). This means

that the resulting image can indeed be used as an environment map for an object in the origin. Spherical environment maps do not have this property; the metal spheres used there have to be assumed small.

Secondly, the sampling rate of a parabolic map varies by a factor of 4 over the complete image (see Heidrich¹³ for a proof). Pixels in the outer regions of the map cover only 1/4 of the solid angle covered by center pixels. This means that directions perpendicular to the viewing direction are sampled at a higher rate than directions parallel to the viewing direction. Depending on how we select mip-map levels, the factor of 4 in the sampling rate corresponds to one or two levels difference, which is quite acceptable. In particular this is somewhat better than the sampling of cubical environment maps.

Parabolic maps can be implemented either by using software for computing the texture coordinates, or by applying special OpenGL extensions. Similar to the cube map extensions, these are now widely available on modern graphics hardware.

2.2. Complex Reflection Models and Environment Map Prefiltering

Once an environment map is available, it can be used to add a mirror reflection term to an object. Using multi-pass rendering and alpha blending, this mirror reflection term can be added to local illumination terms that are generated using hardware lighting. In order to incorporate global illumination with other reflection models than perfect metallic mirrors, we need to perform some precomputations, since real-time calculations are typically not possible due to the high computational cost. The two fundamental techniques for using environment maps with more general reflection models are

- **Decomposition.** The reflection model is decomposed into simpler contributions, which can be treated separately. For example, a reflection model may be separated into a diffuse and a specular term, where the specular term is additionally multiplied with an angular dependent term (Fresnel term).
- **Prefiltering.** For certain reflection models, the reflection of an environment map can be analytically precomputed and stored into a new map. The latter is called *prefiltered environment map* or *reflection map*.

In the following we will describe these two techniques and demonstrate some applications for them.

2.2.1. Decomposition

As stated above, decomposition of a reflection model means separating its terms into simpler expressions that can be handled individually. The most fundamental example is a separation into diffuse and specular contributions. As described below, the diffuse term as well as certain specular terms can

be treated with prefiltering. Another term could be if we had a reflection model with a term for retro-reflection (light that is reflected back into the direction of incoming light). Also an interesting example is the factorization of the specular component into a standard environment map and an angular dependent term (Fresnel term), as described in the following.

Generalized Mirror Reflections using a Fresnel Term

The Fresnel term is a physical term describing the reflectivity of a material depending on its optical density n (“index of refraction”) and the angle of incoming light. It is given as

$$F = \frac{(g - c)^2}{2(g + c)^2} \left[1 + \frac{c(g + c) - 1}{(c(g - c) + 1)^2} \right], \quad (1)$$

with $c = \langle \vec{n}, \vec{v} \rangle$ and $g^2 = n^2 + c^2 - 1$.

A regular environment map without prefiltering describes the incoming illumination at a point in space. If this information is directly used as the outgoing illumination, as is described above, then only surfaces with a constant Fresnel term (i.e. metals) can be modeled.

For non-metallic materials (materials with a small optical density), however, the reflectance strongly depends on the angle of the incoming light. Mirror reflections on these materials should be weighted by the Fresnel term for the angle between the normal and the reflected viewing direction \vec{r}_v .

For any given material, the Fresnel term $F(\cos \theta)$ for the mirror direction \vec{r}_v can be stored in a 1-dimensional texture map¹², and rendered to the framebuffer’s alpha channel in a separate rendering pass. The mirror part is then multiplied with this Fresnel term in a second pass, and a third pass is used to add the diffuse part. If we have a reflection model consisting of a mirror component L_m and a diffuse component L_d , this yields an outgoing radiance of $L_o = F \cdot L_m + L_d$.

In addition to simply adding the diffuse part to the Fresnel-weighted mirror reflection, we can also use the Fresnel term for blending between diffuse and specular: $L_o = F \cdot L_m + (1 - F)L_d$. This allows us to simulate diffuse surfaces with a transparent coating: the mirror term describes the reflection off the coating. Only light not reflected by the coating hits the underlying surface and is there reflected diffusely.

Figure 3 shows images generated using these two approaches. In the top row, the Fresnel-weighted mirror term is shown for indices of refraction of 1.5, 5, and 200. In the center row, a diffuse term is added, and in the bottom row, mirror and diffuse terms are blended using the Fresnel term. Note that for low indices of refraction, the object is only specular for grazing viewing angles, while for a high indices of refraction we get the original metal-like reflection.

2.2.2. Prefiltered Environment Maps

Generally speaking, prefiltered environment maps capture all the reflected exitant radiance towards all directions \vec{v} from a fixed position \mathbf{x} :

$$L_o(\mathbf{x}; \vec{v}, \vec{n}, \vec{l}) = \int_{\Omega} f_r(\vec{w}(\vec{v}, \vec{n}, \vec{l}), \vec{w}(\vec{l}, \vec{n}, \vec{l})) L_i(\mathbf{x}; \vec{l}) < \vec{n}, \vec{l} > d\vec{l}, \quad (2)$$

where \vec{v} is the viewing direction and \vec{l} is the light direction in world-space, $\{\vec{n}, \vec{l}, \vec{n} \times \vec{l}\}$ is the local coordinate frame of the reflective surface, $\vec{w}(\vec{v}, \vec{n}, \vec{l})$ represents the viewing direction and $\vec{w}(\vec{l}, \vec{n}, \vec{l})$ the light direction relative to that frame, f_r is the BRDF, which is usually parameterized via the local viewing and light direction.

A prefiltered environment map stores the radiance of light reflected towards the viewing direction \vec{v} , which is computed by weighting the incoming light L_i from all directions \vec{l} with the BRDF f_r . Note, that L_i is stored in the unfiltered original environment map. As you can see, in the general case we have a dependence on the viewing direction as well as on the orientation of the reflective surface, i.e. the local coordinate frame $\{\vec{n}, \vec{l}, \vec{n} \times \vec{l}\}$.

This general kind of map is five-dimensional. Two dimensions are needed to represent the viewing direction \vec{v} (a unit vector in world coordinates) and three dimensions are necessary to represent the coordinate frame $\{\vec{n}, \vec{l}, \vec{n} \times \vec{l}\}$; e.g. three Euler angles can be used to specify the orientation of an arbitrary coordinate frame (e.g.¹⁴).

Of course, five-dimensional tables have enormous memory requirements, which is why in practice some dependencies (e.g. the tangent \vec{l}) are dropped, and why prefiltered environment maps are often reparameterized (e.g. indexing is not done with the viewing direction \vec{v} , but the reflected viewing direction). Because this reduction in dimensionality also removes some to the generality of the approach, the decomposition method is often required to combine several of these simplified models.

If the original environment map is given in a high-dynamic range format¹⁵, then the prefiltering technique allows for effects similar to the ones described by Debevec¹⁶.

Diffusely Prefiltered Maps As we have seen, we can combine a mirror reflection term using an environment map with local illumination terms that are generated using hardware lighting. It is also possible to add a diffuse global illumination term through the use of a precomputed texture. For the generation of such a texture, there are two methods. In the first approach, a global illumination algorithm such as Radiosity is used to compute the diffuse global illumination of every surface point.

The second approach is purely image-based, and uses a prefiltered environment map^{17, 9}. A traditional environment map used for the mirror term contains information about the incoming radiance $L_i(\mathbf{x}, \vec{l})$, where \mathbf{x} is the point

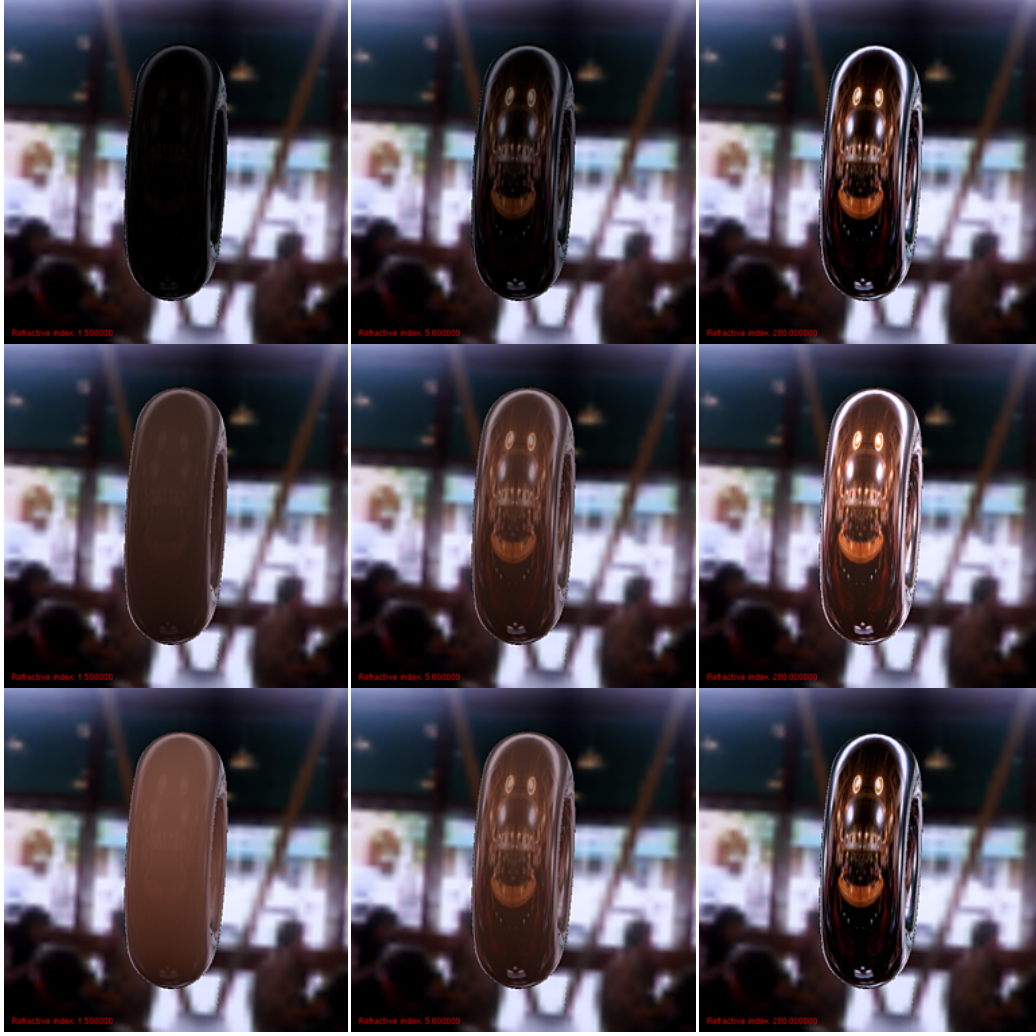


Figure 3: Top row: Fresnel weighted mirror term. Center row: Fresnel weighted mirror term plus diffuse illumination. Bottom row: Fresnel blending between mirror and diffuse term. The indices of refraction are (from left to right) 1.5, 5, and 200.

for which the environment map is valid, and \vec{l} the direction of the incoming light. The outgoing radiance for a diffuse BRDF is then:

$$L_o(\mathbf{x}, \vec{n}) = k_d \cdot \int_{\Omega(\vec{n})} L_i(\mathbf{x}, \vec{l}) \cdot \cos(\vec{n}, \vec{l}) d\omega(\vec{l}). \quad (3)$$

Due to the constant BRDF of diffuse surfaces, L_o is only a function of the surface normal \vec{n} and the illumination L_i stored in the environment map, but not of the outgoing direction \vec{v} . Thus, it is possible to precompute a map containing the diffuse illumination for all possible surface normals. For this map, like for the mirror map, any parameterization from Section 2.1 can be used. Figure 4 shows such a prefiltered map, a torus with diffuse illumination

only as well as a torus with diffuse and mirror illumination.

Glossy Prefiltering of Environment Maps A simplification similar to the one used for diffuse materials is also possible for certain specular reflection models^{12, 17}, most notably the Phong model. Voorhies et al.¹⁰ used a similar approach to implement Phong shading for directional light sources.

As shown by Lewis¹⁸, the Phong BRDF is given by

$$f_r(\mathbf{x}, \vec{l} \rightarrow \vec{v}) = k_s \cdot \frac{\langle \vec{r}_l, \vec{v} \rangle^{1/r}}{\cos \alpha} = k_s \cdot \frac{\langle \vec{r}_v, \vec{l} \rangle^{1/r}}{\cos \alpha}, \quad (4)$$

where \vec{r}_l , and \vec{r}_v are the reflected light- and viewing directions, respectively, and $\cos \alpha = \langle \vec{n}, \vec{l} \rangle$. Thus, the specular



Figure 4: Left: diffusely prefiltered environment map of the cafe scene. Center: diffusely illuminated torus. Right: same torus illuminated with both a diffuse and a mirror term.

global illumination using the Phong model is

$$L_o(\mathbf{x}, \vec{r}_v) = k_s \cdot \int_{\Omega(\vec{n})} \langle \vec{r}_v, \vec{l} \rangle^{1/r} L_i(\mathbf{x}, \vec{l}) d\omega(\vec{l}), \quad (5)$$

for some roughness value r . This is only a function of the reflection vector \vec{r}_v and the environment map containing the incoming radiance $L_i(\mathbf{x}, \vec{l})$. As for diffuse illumination, it is therefore possible to take a map containing $L_i(\mathbf{x}, \vec{l})$, and generate a filtered map containing the outgoing radiance $L_o(\mathbf{x}, \vec{r}_v)$ for a glossy Phong material.

Figure 5 shows such a map, as well as a glossy sphere and torus textured with this map.

A Fresnel weighting of these prefiltered environment maps similar to the way it is described above is only possible with approximations. The exact Fresnel term for the glossy reflection cannot be used, since this term would have to appear inside the integral of Equation 5. However, for glossy surfaces with a low roughness, the Fresnel term can be assumed constant over the whole specular peak (which is very narrow in this case). Then the Fresnel term can be moved out of the integral, and the same technique as for mirror reflections applies.

The use of a Phong model for the prefiltering is somewhat unsatisfactory, since this is not a physically valid model. However, this method works for all reflection models having lobes that are rotationally symmetric about the reflected viewing direction, and whose shape does not depend on the angle to the surface normal.

Approximations of General Isotropic BRDFs Based on this concept, Kautz and McCool¹⁹ extended the Phong environment maps idea to other isotropic BRDFs by approximating them with a special class of BRDFs:

$$f_r(\vec{v}, \vec{l}) := p(\langle \vec{n}, \vec{r}_v(\vec{n}) \rangle, \langle \vec{r}_v(\vec{n}), \vec{l} \rangle),$$

where p is an approximation to a given isotropic BRDF, which is not only isotropic, but also radially symmetric about $\vec{r}_v(\vec{n}) = 2(\vec{n} \cdot \vec{v})\vec{n} - \vec{v}$, and therefore only depends on two parameters.

Now consider Equation 2 using this reflectance function:

$$L_o(\mathbf{x}; \vec{v}, \vec{n}, \vec{l}) = \int_{\Omega(\vec{n})} p(\langle \vec{n}, \vec{r}_v(\vec{n}) \rangle, \langle \vec{r}_v(\vec{n}), \vec{l} \rangle) \cdot L_i(\mathbf{x}; \vec{l}) \langle \vec{n}, \vec{l} \rangle d\omega(\vec{l}). \quad (6)$$

The authors then make the assumption that the used BRDF is fairly specular, i.e. the BRDF close to zero almost everywhere, except for $\vec{r}_v(\vec{n}) \approx \vec{l}$. Using this assumption they reason that $\langle \vec{n}, \vec{r}_v(\vec{n}) \rangle \approx \langle \vec{n}, \vec{l} \rangle$. Now the equation can be reparameterized and rewritten the following way:

$$L_o(\mathbf{x}; \vec{r}_v, \langle \vec{n}, \vec{r}_v \rangle) = \int_{\Omega(\vec{n})} p(\langle \vec{n}, \vec{r}_v \rangle, \langle \vec{r}_v, \vec{l} \rangle) \cdot L_i(\mathbf{x}; \vec{l}) d\omega(\vec{l}), \quad (7)$$

which is three dimensional. The third dimension is used to vary the diameter of the lobe with the angle between reflection vector and surface normal. This way, it is possible to have materials that are almost mirror-like at grazing viewing angles, while they are matte if looked at perpendicularly. This is a behavior that can be seen quite often with real materials.

In addition to this, Kautz and McCool also proposed an approximation technique that generates a BRDF with rotationally symmetric lobes from an arbitrary BRDF. This is done by averaging the lobes for different viewing directions.

This technique has the advantage that it can use approximations of arbitrary isotropic BRDFs and achieves interactive frame rates. Off-specular peaks can also be incorporated into this technique. Additional Fresnel factors like Miller¹⁷ and Heidrich¹² proposed are not required because they can be incorporated into the dependency on the viewing angle, i.e. the third dimension of the map. On the



Figure 5: A prefiltered version of the map with a roughness of 0.01, and application of this map to a reflective sphere and torus.

down side, 3D textures are quite space consuming and are not supported by most current low-end hardware.

Depending on the BRDF, the quality of the approximation varies. For higher quality approximations Kautz and McCool also propose to use a multilobe approximation, which basically results in several prefiltered environment maps that have to be added.

For instance, if the BRDF consists of several separate surface phenomena (e.g. retro-reflections, diffuse reflections, and glossy reflections), each part has to be approximated separately since no radially symmetric approximation can be found for the whole BRDF. This again means a decomposition of the reflection model into several parts.

Warping for Environment Maps with Isotropic BRDFs

A different technique which makes similar assumptions (isotropic and radially symmetric BRDF) was presented by Cabral et al.²⁰. They prefilter an environment map for different fixed viewing directions, resulting in view-dependent, spherical environment maps. An alternative to the prefiltering process is to take photographs from different viewing directions of a sphere made of the same material one would like to represent.

In contrast to the previous approach, this is actually a four-dimensional environment map

$$L_o(\mathbf{x}; \vec{v}, \vec{n}) = \int_{\Omega(\vec{n})} p(\langle \vec{n}, \vec{r}_v \rangle, \langle \vec{r}_v, \vec{l} \rangle) \cdot L_i(\mathbf{x}; \vec{l}) \cdot d\omega(\vec{l}), \quad (8)$$

but the two dimensions representing the viewing direction \vec{v} are only sampled very coarsely. A different two dimensional spherical map is extracted from this four-dimensional map for every new viewpoint. This map corresponds to one specific viewing direction and is generated using warping. The new view-dependent environment map is then applied to an object. The warping compensates for the undersampled viewing directions, and minimizes the visible artifacts. Although the warping re-

quires high-end graphics hardware to achieve interactive frame rates, the final rendering can be done with standard sphere mapping, which is major the reason for generating the intermediate spherical map.

Warping is done based on an assumption what the central reflection direction of the BRDF is (the reflected viewing direction and the surface normal are mentioned as examples in the original paper²⁰). For example, if a specular highlight is assumed, then the warping is performed such that the location of the highlights are located in the same position after warping to the destination direction. The assumption of a single, predominant reflection direction fails for BRDFs that have off-specular reflections like strong diffuse components or retro-reflection. Similarly, since radially symmetric BRDFs are used, this method has the same difficulties with complex BRDFs as the previous method. To overcome these problems, the method can be combined with a decomposition approach.

As mentioned before the generated two dimensional environment map is view-dependent, so the reflective object needs to be viewed with an orthographic projection or otherwise the reflections are incorrect, since the reflection directions are computed based on an infinite viewer. For example, if the material contains a strongly varying Fresnel term, it cannot be represented in this form, because the spherical map does not depend on the angle between normal and light direction.

Hardware Accelerated Prefiltering For interactive applications it would be nice if environment map prefiltering could be done on the fly. This means that if the scene changes, glossy reflections change accordingly. Here, a method by Kautz et al.²¹ to perform hardware-accelerated Phong filtering of a given environment map is described. In a prefiltered environment map, every texel is a weighted sum of all pixels in a source environment map. This means, we can think of the filtering process as applying a (BRDF-dependent) filter kernel to some unfiltered source map. We would like to map this filtering operation to the operations provided by a graphics hardware pipeline. The

OpenGL imaging subset only supports shift-invariant two dimensional filters of certain sizes, and we would like to use this feature to perform the filtering. Hence, for hardware accelerated prefiltering we have to choose an environment map technique that uses only two dimensional environment maps with a BRDF that results in a shift-invariant filter over the hemisphere, and an environment map parameterization that keeps the filter shift-invariant. As shown by Kautz et al.²¹, the parabolic map comes closest to these demands. Combined with any kind of symmetric lobe BRDF (e.g. Phong), the prefiltering can be mapped to hardware convolutions, which allows for prefiltering at interactive frame rates. This enable on-the-fly generation of prefiltered environment maps for rendering glossy global illumination in dynamic environments.

2.3. Discussion

The problem of the environment map approach is that all objects are assumed infinitely small and distant to the environment. This means that the parallax that can be observed for large objects, and especially large planar reflectors, cannot be correctly simulated with environment maps. Nonetheless, environment maps as well as decomposition and prefiltering are the most commonly used approach for rendering non-diffuse global effects in highly interactive applications today. This includes both games and a variety of virtual reality systems.

3. Light Fields and Lumigraphs

In order to correctly account for the parallax effects that the environment map approach cannot handle, we require one environment map for each point in space (or at the very least for each point on the surface of the reflective object).

This is the fundamental idea of light fields. A light field²² is a 5-dimensional function describing the radiance at every point in space in each direction. It is closely related to the *plenoptic function* introduced by Adelson²³, which in addition to location and orientation also describes the wavelength dependency of light.

In the case of a scene that is only to be viewed from outside a convex hull, it is sufficient to know what radiance leaves each point on the surface of this convex hull in any given direction. Since the space outside the convex is assumed to be empty, and radiance does not change along a ray in empty space, the dimensionality of the light field can be reduced by one, if an appropriate parameterization is found. The so-called two-plane parameterization fulfills this requirement. It represents a ray via its intersection points with two parallel planes. Several of these pairs of planes (also called *slabs*) are required to represent a complete hull of the object. Since each of these points is characterized by two parameters in the plane, this results in a 4-dimensional

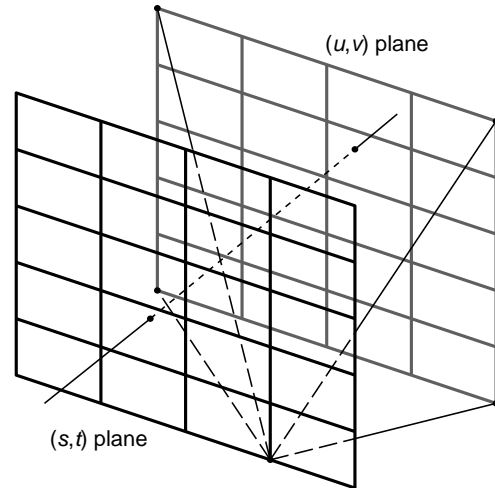


Figure 6: A light field is a 2-dimensional array of images taken from a regular grid of eye points on the (s, t) -plane through a window on the (u, v) -plane. The two planes are parallel, and the window is the same for all eye points.

function that can be densely sampled through a regular grid on each plane (see Figure 6).

One useful property of the two-plane parameterization is that all the rays passing through a single point on the (s, t) -plane form a perspective image of the scene, with the (s, t) point being the center of projection. Thus, a light field can be considered a 2-dimensional array of perspective projections with eye points regularly spaced on the (s, t) -plane. Other properties of this parameterization have been discussed in detail by Gu et al.²⁴.

Since we assume that the sampling is dense, the radiance along an arbitrary ray passing through the two planes can be interpolated from the known radiance values in nearby grid points. Each such ray passes through one of the grid cells on the (s, t) -plane and one on the (u, v) -plane. These are bounded by four grid points on the respective plane, and the radiance from any of the (u, v) -points to any of the (s, t) -points is stored in the data structure. This makes for a total of 16 radiance values, from which the radiance along the ray can be interpolated quadri-linearly. As shown in by Gortler et al.²⁵ and Sloan et al.²⁶, this algorithm can be considerably sped up by the use of texture mapping hardware. Sloan et al.²⁶ also propose a generalized version of the two-plane parameterization, in which the eye points can be distributed unevenly on the (s, t) -plane, while the samples on the (u, v) -plane remain on a regular grid.

Other parameterizations for the light field have been proposed by several authors^{27, 28} in order to achieve a better sampling uniformity. However, except for surface light fields (Section 3.2), these are not of great practical importance since the reconstruction time for the radiance along any

given ray can no longer be done in constant time as with the regular grid in the two-plane parameterization.

3.1. Lumigraphs: Light Fields Plus Geometry

The quadri-linear interpolation in the light field data works well as long as the resolution of the light field is high. For low resolutions, the interpolation only yields a sharp image for objects in the (u, v) -plane. The further away points are from this plane, the more blurred they appear in the interpolated image.

The Lumigraph²⁵ extends the concept of a light field by adding some geometric information that helps compensating for this problem. A coarse polygon mesh is stored together with the images. The mesh is used to first find the approximate depth of the object along the ray to be reconstructed, and then this depth is used to correct the weights for the interpolation. This will reduce the ghosting artifacts for the geometry itself. However, in the case of very shiny materials, the reflections will still exhibit some amount of ghosting, since the depth correction is performed for the geometry and not for the apparent depth of the object seen in the reflection. This is a problem that none of the light field or Lumigraph methods can solve at the moment.

Heidrich et al.²⁹ take a similar, but purely sampling-based approach. Instead of a polygon mesh, the depth of each pixel in the light field is stored. This information is then used to refine the light field with warped images until the rendering quality is satisfactory. This decouples the more expensive depth correction from the efficient quadri-linear interpolation, and thus can be used to achieve higher frame rates. This basic idea of a sampling-based representation for the geometry has since been used for adaptive acquisition of light fields³⁰ and a high-quality, warping-based reconstruction instead of the quadri-linear interpolation³¹.

Recently, Isaksen et al.³² have proposed a more sophisticated reconstruction scheme, which involves information not only from the closed eye points, but from all eye points within a certain perimeter of the ray intersection with the (s, t) -plane. This user defined perimeter defines a synthetic aperture that is used for reconstructing the image. Furthermore, Isaksen et al. propose to dynamically reparameterize the light field to use depth correction with different focal planes. Since different focal planes can be used for different parts of the images, this defines a smooth transition between the original light field work²², and the original Lumigraph approach using a geometric model²⁵. By using the synthetic aperture camera, ghosting can be replaced by blurring for object located away from the focal geometry.

Also in a recent paper, Chai et al.³³ explored the sampling-theoretic resolution of light fields necessary to represent scenes with a given dynamic range of depth values without blurring or ghosting. An interesting result of their work

is that the necessary sampling rate can be reduced dramatically by the introduction of a small amount of additional depth information as proposed by Heidrich et al.²⁹. In particular, their results show that a few bits of quantized per-pixel depth values are sufficient as long as the quantization is not done in a linear, but in a hyperbolic fashion.

3.2. Surface Light Fields

If we take the concept of combining geometry and light field data to its extremes, we arrive at the original geometric model of the object. Instead of parameterizing the ray space using intersections with virtual geometry (such as a light slab in the case of the two-plane parameterization), we can then reparameterize the light field to use the 2D surface position on the original geometry as two of the four parameter values. The remaining two directions would then parameterize the hemisphere of directions over the tangent plane of that surface point. This concept is called a *surface light field*³⁴.

In other words, a surface light field is a 4D data structure which describes for every point on a surface parameterized over a 2D parameter domain u, v , which radiance leaves that surface point for all possible directions (parameterized over s, t). In order to render an image of the object, we then have to first compute the intersection of the ray with the original geometry, and then reconstruct the radiance for that intersection point and viewing direction by quadri-linear interpolation. Miller et al.³⁴ describe both a specific parameterization for the directions, as well as a way of partially exploiting the graphics hardware for doing the interpolation.

While Miller et al. use synthetically generated surface light fields for parametric objects, Wood et al.³⁵ describe in a recent paper how to acquire surface light fields from real world objects. They generate a set of so-called *lumispheres* for a dense set of surface points by using techniques from mesh simplification and surface fairing. They also describe how to compress the resulting data set, which will be described in more detail below. In order to arrive at a parameterization for the geometry, which may be a polygonal model of arbitrary topology, Wood et al. use the MAPS algorithm by Lee et al.³⁶.

The obvious advantage of the surface light field approach is that images rendered in this fashion will always show sharp geometry, although reflections may still exhibit ghosting as described above. The downside of the surface light field approach is that the rendering time is no longer independent of geometric complexity, which is usually considered one of the most interesting features of image-based rendering in general.

3.3. Illumination From Light Fields

Instead of using light fields or Lumigraphs directly for viewing, it is also possible to use them for illumination purposes

only. An example of such an algorithm is the *canned light source* approach³⁷, where complex luminaries with strongly varying spatial and directional light distributions are stored in a light field data structure. Such a canned light can then later be used for illuminating arbitrary objects, for example in a ray-tracing step, but also in hardware-accelerated rendering.

Another example is the rendering of refractive objects using light field representation for storing geometric information³⁸. In this work, a two-plane parameterized light field of a refractive object stores the refracted ray leaving the object for every incident viewing ray. In this way, the geometry-dependent visibility information is precomputed and stored in a light field data structure. At rendering time, the object is displayed using the normal light field rendering algorithm, yielding an image representing the refracted ray for every pixel. For each of these pixels, the illumination along that ray is then looked up either from an environment map or from another light field. Thus, the geometry is decoupled from the illumination, and both can be exchanged independently.

3.4. Compression of Light Fields

Since the size of light field data sets can easily exceed several Gigabytes, several researchers have worked on compression schemes to make light fields more practical. For efficient rendering it is usually desirable to have the possibility for random access to individual samples, and constant time reconstruction of the radiance along a given ray. This is the case for the two-plane parameterized light field, but difficult to achieve in combination with a good compression scheme.

The first compression scheme for light fields was vector quantization, and was presented in the original paper by Levoy and Hanrahan²². Later, a hardware-accelerated form of reconstruction for vector-quantized light fields was presented³⁸. In the compression scheme proposed by Levoy and Hanrahan, blocks of adjacent light field samples (e.g. blocks of 2^4 pixels) are concatenated to form vectors. Each block is then replaced by a 16-24 bit index into a vector table describing the radiance along all rays between points in the vector. This gives moderate compression ratios of about 24:1, depending on the exact size of the table and the blocks, but constant reconstruction time is maintained.

Wood et al.³⁵ have extended the vector quantization approach to surface light fields. Here, the reconstructed lumispheres (see Section 3.2) are quantized after some transformations that try to increase the similarity between the different spheres. Since the lumispheres are actually continuous functions rather than vectors, Woo et al. call their approach *function quantization* rather than vector quantization. Similarly, they propose a method they call *principal function analysis* (which is a generalization of principal component analysis) that actually interpolates between the vectors stored in the vector table.

Better compression ratios can be achieved by block based coding with motion prediction similar to the MPEG and H263 methods for video compression. Such methods have been introduced by Miller et al.³⁴ for surface light fields, and by Magnor and Girod³⁹ for two-plane parameterized light fields. This maintains a constant reconstruction time, but since a whole block is decompressed at once, a sequential reconstruction is faster than random access.

Finally, Lalonde and Fournier⁴⁰ have worked on wavelet compression for light fields. The compression ratios reported for their scheme are interesting, but reconstruction time is logarithmic rather than constant, and in terms of absolute rendering times the reconstruction takes significantly longer than the other methods.

3.5. Discussion

In summary, it can be seen from the variety of approaches, that light fields are becoming a relatively mature way of representing objects including their illumination. We are starting to see some theoretical analysis of the properties of different light field representations, as well as a toolbox of different light field techniques that are available for different problem settings. Unfortunately, the memory consumption has so far limited the use of light fields in practical applications, but with the recent advances in compression techniques, it is to be expected that this will change in the future.

4. Sparse, Light Field-Like Representations

The representations of illumination used by the methods described in this section can be interpreted as light fields although the authors of the work have not originally described their algorithms in this fashion. In contrast to the techniques from Section 3, the methods described here use a sparser, less regular representation of the light field information. This results in significantly reduced storage costs, but also in a more expensive reconstruction step. In addition, the sparse sampling of the light field typically means that less spatial or directional detail can be preserved.

4.1. View-Dependent Vertex Colors

A simple method for interactive viewing of precomputed global illumination solutions is to extract the view-dependent color for each vertex of a polygonal model from the illumination solution, and then use graphics hardware to render the model with Gouraud shading. In order to facilitate view-dependent per-vertex computations, the illumination should be stored in a fashion that makes this operation as efficient as possible.

Stamminger et al.⁴¹ propose the *illumination sample* method for generating the global illumination solution in the first place. This algorithm is a radiance clustering method that efficiently represents incoming illumination at patches.

After the solution has been computed, this representation is transformed into a directional representation of the illumination at the vertices of the polygonal model. A Haar wavelet basis was chosen by Stamminger et al. for storing the directional information. This approach can be interpreted as a surface light field where the spatial samples are located at vertices only, and the directional samples are projected into a wavelet basis.



Figure 7: An example of the algorithm by Stamminger et al.⁴¹. Image courtesy of Marc Stamminger.

At rendering time, the color at each vertex has to be determined for the current viewing direction by reconstructing the outgoing radiance towards the viewer from the wavelet representation. Since this can be quite costly to do for every vertex, a threshold for the change in viewing direction is introduced, below which the color from the previous frame is reused. Because the lighting is per-vertex, the spatial resolution of the reconstructed illumination is typically fairly low, especially compared to the light field methods from Section 3.

4.2. Interactive Display of Photon Maps

A scattered representation of the light arriving at a surface has been proposed by Shirley et al.⁴². Photons are traced from the light sources, and reflected or refracted via specular surfaces. The density of the photon hits is later used to estimate the local radiance distribution at a surface point (density estimation). Since the photons are traced stochastically, both the points where they hit an object, and their incoming direction at that point is random. This corresponds to a scattered data representation of the light field arriving at the surfaces in the scene.

Stürzlinger and Bastos⁴³ proposed an interactive viewing algorithm for displaying the results of this simulation, which we will describe in the following. Like Shirley et al.⁴², Stürzlinger and Bastos use splatting of the individual

photons for the density estimation step. To this end, they choose an object-space filter kernel, which they store in a 2-dimensional texture map. Then they render each individual photon as an object-space triangle with that texture applied. In order to account for view-dependent effects, the splat for each photon has to be weighted by the BRDF value for the given viewing direction and the direction of the incoming photon, which is computed on the fly in software.

To improve the visual quality of the rendering method, Stürzlinger and Bastos⁴³ extend this basic algorithm such that direct illumination is performed by hardware lighting combined with shadow maps, and the photons are only used for rendering the indirect light contributions. The resulting method produced near-interactive frame rates for moderately complex scenes on high-end graphics hardware.

4.3. Virtual Lights

Another branch of research for interactively displaying indirect illumination is the fitting of virtual lights to previously obtained global illumination solutions. Different sets of virtual lights are computed for each of the objects in the scene or even for different parts of an object. Each set of lights is only active while the respective object or object part is rendered. These virtual lights allow for the use of graphics hardware combined with a Phong reflection model for approximating the true indirect illumination of the object. One could interpret this approach as a highly compressed representation for surface light fields, where each virtual light corresponds to a beam of incident light on the surface. Therefore, the spatial resolution of the illumination is high (the reflection can be computed at every pixel of the final image), but the directional sampling is limited by the number of light sources used.

The first work based on this general idea was presented by Stamminger et al.⁴⁴. They obtained their global illumination solution with a Wavelet Radiance method⁴⁵, a generalization of Wavelet Radiosity⁴⁶ to non-diffuse environments. The link structure of the Wavelet Radiance solution gives an indication which objects or patches in the scene send the most energy towards any given object. The brightest of these patches are then replaced by virtual point lights whose brightness is set according to the energy exchanged between the patch and the object. An example of this method is shown in Figure 8. This image shows the complexity of scenes that could be handled by the Wavelet Radiance methods that were state-of-the-art at that time. The actual interactive display algorithm could also handle more complex scenes.

The second approach, presented by Walter et al.⁴⁷ starts with a global illumination solution provided in the form of a surface light field. For a collection of points or vertices on the object, for which the outgoing radiance is known, the authors greedily fit a number of Phong lobes corresponding to the effect of directional light sources. Since Phong lobes are

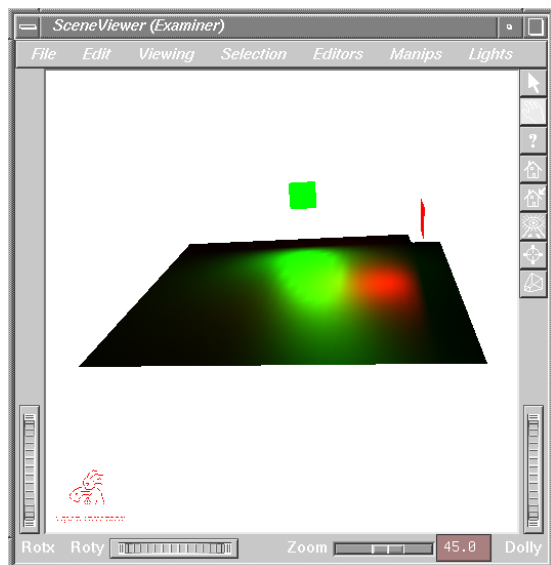


Figure 8: An example of the virtual light fitting method by Stamminger et al.⁴⁴. Image courtesy of Marc Stamminger.

positive everywhere, it is not possible to subtract energy that has once been added. This complicates the fitting process.

Both the approach from Stamminger et al.⁴⁴ and Walter et al.⁴⁷ suffer from the fact that graphics hardware supports only a very small number of light sources, typically 8. This means that detailed reflection patterns cannot be represented with this method, except when the set of virtual light sources is chosen for very small geometric entities, such as polygons. In that case, however, the parameters of the light sources have to be changed frequently, which is a slow operation on graphics hardware, and is thus only feasible for small scenes.

4.4. Instant Radiosity

Instant Radiosity⁴⁸ is an approach that also uses virtual light sources, but on a global scale rather than different lights for each of the objects in the scene. As the name suggests, the basic method has been developed for diffuse scenes, but the paper also describes an extension to glossy environments.

The core of the method is to trace the path of photons emitted from a light source with a quasi-random walk. In a diffuse scene, a virtual point light is placed wherever the photon hits a surface. This light represents the light reflected from that point in all directions. In a specular scene, light should only be reflected in a specific direction. This is achieved by reflecting the origin of the ray from which the photon arrived at the surface that was hit by the photon, and placing a light source there. The effect of the light source is then clamped to the region contained in the generalized pyramid from the light position through the boundaries of the polygon.

Since virtual lights affect all objects in the scene in an Instant Radiosity implementation, shadowing effects have to be taken into account. Keller⁴⁸ solves this by implementing a shadow map approach described in⁴⁹. To account for dynamic environments, Keller suggests to replace a subset of the photon paths for every frame. This is a relatively cheap operation since only a few rays have to be traced.

4.5. Discussion

We have seen that several interactive rendering algorithms exist that are based on sparse, light field like representations. From the discussion, it is quite obvious that each of the algorithms uses a different, specialized representation for storing the global illumination solution. The relationship between these different representations and their tradeoffs in terms of storage and quality are not well understood at this point. A general theory of sparse light field representations is currently not available.

5. On-The-Fly Computation

The methods described so far have all been based on pre-computed global illumination solutions. As a consequence, most of them are not well suited for dynamic environments (with the exception of the hardware-accelerated prefiltering of environment maps, Section 2.2.2, as well as Instant Radiosity, Section 4.4). In this section, we describe methods for computing certain light paths in real time. This includes both specialized methods for very specific geometry and materials, as well as general solutions based on ray-tracing.

5.1. Mirror Reflections in Planar or Slightly Curved Geometry

A commonly used technique for rendering mirror reflections on planar objects is given by Diefenbach^{50, 51}: with a simple affine model/view matrix, the scene is mirrored at the planar reflector. This mirrored scene is rendered at every pixel where the reflector is visible in the current view. This is typically achieved in two rendering passes. First, the original scene is rendered, and all pixels of the planar reflector are marked in the stencil buffer. Then, the model/view matrix is modified to accommodate for the reflection. The scene is now rendered again, but only pixels marked in the stencil buffer are set. If the stencil buffer has more than one bit, it is also possible to realize multiple reflections by recursing the procedure⁵¹.

A similar effect can be achieved using texture mapping. Instead of mirroring the scene, the eye point \mathbf{p} is mirrored, yielding a reflected eye point \mathbf{p}' , as depicted on the left side of Figure 9. Rendering the scene from this eye point with the reflector as an image plane yields the texture image to be applied to the reflector as seen from the eye. Note that this approach has two major disadvantages compared to the one

from Diefenbach. Firstly, the rendered image from the first pass needs to be transferred from the framebuffer into texture memory, which requires additional bandwidth, and secondly, the texturing represents a resampling step that reduces image quality.

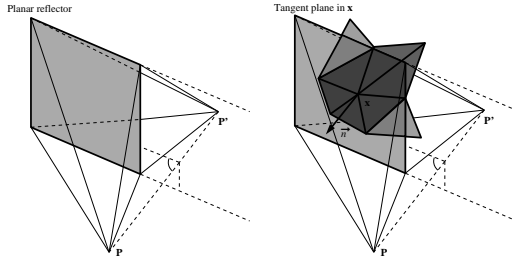


Figure 9: Multi-pass mirror reflections in planar and curved objects. While a single reflected eye point p' exists for planar reflectors, curved reflectors do not have such a uniquely defined point. If a curved object is approximated by a triangle mesh with per-vertex normals, one reflected point can be defined for each vertex in the mesh using the tangent plane in that vertex.

5.1.1. Glossy Reflection for Planar Reflectors

For these reasons, the modified algorithm is an inferior choice for implementing reflections on planar surfaces, but it is useful for approximating glossy reflections. Bastos et al.^{52, 53} propose to convolve the texture (which they generate with an image-based warping step rather than a geometry-based rendering) with a space-invariant filter kernel corresponding to the BRDF.

This is similar in spirit to the prefiltering approach described in Section 2.2.2, but since the filter is space-invariant, an orthographic viewer is implicitly assumed for the prefiltering. This will produce artifacts for large reflectors or wide angle cameras. In addition to prefiltering, Bastos et al.^{52, 53} also use decomposition, as explained in Section 2.2.1, since they also separate the Fresnel term from the BRDF and apply it in a separate rendering pass using texture mapping.

An alternative to using hardware convolution, is to apply Diefenbach's algorithm from Section 5.1 multiple times with slightly jittered reflected geometry⁵¹. This jittering should correspond to the distribution of microfacet normals on the glossy surface. Unfortunately, for achieving a high rendering quality, a lot of rendering passes are required, resulting in a low performance.

5.1.2. Texture-Based Rendering of Curved Mirrors

Based on the texture-based rendering approach for planar mirrors described above, we can also develop a naive (and inefficient) method for generating reflections on curved surfaces represented as triangle meshes: for curved surfaces the

problem is that the reflected eye point is not constant, but varies across the surface. However, if the surface is reasonably smooth, then it suffices to compute the reflected eye point only at some discrete points on the surface, say the vertices of the triangle mesh, and to interpolate the radiance for each point inside a triangle from the textures obtained for each of the three vertices. Note that each of the textures corresponds to a dynamically generated, 2-dimensional slice of a light field describing the incoming illumination around the reflector, and the interpolation step is nothing but the reconstruction of a novel view from this light field information.

The complete algorithm would then work as follows (see right side of Figure 9): For each vertex in the triangle mesh the tangent plane is determined, the eye point is reflected in that plane, and the reflection texture for that tangent plane is rendered. Then, for each vertex, the triangle fan surrounding it is rendered with the reflection applied as a projective texture. During this rendering, the alpha value for the center vertex of the fan is set to 1, the alpha values for all other vertices are set to 0, and the result from texturing is multiplied by the alpha channel. This way, the alpha channel contains the basis functions for the Barycentric coordinates in each pixel. The final image results from adding up all the contributions from the different triangle fans in the frame buffer. This is exactly the interpolation scheme used for the hardware implementation of light fields and Lumigraphs.^{25, 26}

Clearly, this approach is not feasible for real time or interactive applications, since the number of vertices (and thus the number of rendering passes) on typical reflectors are often in the order of tens of thousands. On the other hand, for a static scene the incoming light field at the object does not change. Therefore, it is not necessary to rerender the geometry multiple times for each frame in order to generate the 2D slices used as textures. Instead, a practical light field-based method could rely on some amount of precomputation to achieve interactive frame rates.

5.1.3. Geometry-Based Rendering of Curved Mirrors

A geometry-based method for reflections on curved surfaces has recently been introduced by Ofek and Rappoport⁶⁴. For each frame, all vertices of the reflected geometry are individually transformed in software to form a virtual reflected object. To this end, it is necessary to determine the point on the reflector, on which the reflection of the vertex is visible. This is done by testing all triangles on the reflector. For every eye point, each reflector triangle with per-vertex normal defines a 3D region, called *reflected cell*, in which 3D geometry reflected via this triangle can reside. Once the triangle on which the reflection occurs has been determined, the location of the exact reflection point can be found, and finding the virtual vertex position from that point and its normal is easy. After all vertices of the surrounding environment have been mirrored this way, the resulting virtual object is simply rendered using graphics hardware.

In the case of a convex reflector, the reflected cells of the different reflector triangles do not overlap, so that each vertex of the surrounding geometry maps to exactly one vertex on the virtual object. This corresponds to the fact that only one copy of the surrounding environment can be visible in a convex reflector. Reflections in concave objects can be achieved in a similar fashion, but mixed reflectors of convex and concave regions have to be partitioned into purely convex and purely concave regions first. For partition, there can be one virtual object corresponding to the complete geometry of the surrounding environment.

This approach only works at interactive performance for relatively smooth objects that are either concave or convex. Like the texturing method described above, this geometry-based approach also quickly becomes infeasible for more complex scenes.

5.2. Interactive Ray-Tracing and Ray Caching

The most serious restriction of the methods described so far in Section 5 is that the illumination effects that can be captured are very limited. For every new effect, a completely new, specialized algorithm has to be developed. In contrast, ray-tracing is a very general method that can simulate a wide variety of different illumination effects, especially when combined with stochastic sampling (e.g. distribution ray tracing⁵⁵ or bidirectional path tracing⁵⁶).

In the past few years, CPU performance has grown to a level where it has become possible to perform interactive ray-tracing of non-trivial scenes on large multiprocessor systems. Parker et al.⁵⁷ describe how to make such a system work by carefully optimizing the ray-tracer for the specific caching architecture of the multiprocessor machine, and by applying efficient tests of whether a surface point is in the penumbra or not. Only for points in the penumbra, lots of light source samples are required, while points in the umbra or completely lit points do not require any sampling.

Despite these optimizations and a large number of processors, there will clearly be scene sizes that cannot be handled at interactive frame rates any more. Therefore, Parker et al.⁵⁷ employ frameless rendering⁵⁸ to incrementally update the pixels in a random order instead of updating all pixels in the image, and then displaying the whole image at once. Using these methods, they achieve several frames per second on a 60 processor Onyx2 for fairly complex scenes.

5.2.1. The Holodeck

The holodeck algorithm⁵⁹ combines ray-tracing with a caching of the previously computed rays, so that these can be reused for different views. Rays are generated on the fly and stored in data base. A specific grid data structure is used to store *beams* (rays of light passing through the same cell in the same direction). Over time, the holodeck algorithm

builds up the complete information of a light field. The algorithm as proposed by Larson does not have a notion of moving objects, and continues to reuse rays for an indefinite period of time. Thus, the original algorithm only deals with static scenes, but it has the advantage over light field rendering^{22, 25} that the data is built up incrementally rather than requiring a lengthy precomputation phase.

The rendering using the holodeck algorithm works as follows. For new viewpoint, the display process determines which beams are required to render the image. Then, all rays inside this beam are searched for, first in main memory, then on disk (if rays have been swapped out of a smaller RAM cache), and finally, new sample rays are generated. From all the samples obtained in a certain time budget, an image is reconstructed by rendering the individual samples, and filling the inbetween holes with a Voronoi diagram of the samples.

5.2.2. The Render Cache

A similar caching scheme for dynamic scenes has been proposed by Walter et al.⁶⁰ The entities cached in their system are individual samples of illumination, composed of a 3D point location, color, object and image id (the latter can be used to compute the viewing direction), as well as an age.

The first step in rendering a new frame is to reproject the individual samples to the new viewpoint. In a second phase the image is traversed, and depth culling and hole filling are performed. This process uses heuristics based on strong differences in the depth buffer and object id, to remove distant objects shining through closer geometry. The resulting image can be displayed to the user.

During this second phase, a sampling priority is generated for each pixel in the destination image. It is used to determine the set of rays to be traced or re-traced for the current view. The age of a sample is also taken into account during generation of the priority value. Since only a subset of pixels can be sampled for each frame, an error-diffusion dithering algorithm is used to thin out the samples and to distribute new rays across the image according to the local sampling priority.

5.3. Combined Ray-Tracing and Hardware Rendering

Because pure ray-tracing is still quite expensive and because interactive frame rates can today only be achieved on large multiprocessor machines, a natural solution is to use graphics hardware for rendering those parts it can deal with, and then only using ray-tracing for filling in those parts that the hardware cannot handle. These approaches will be summarized in the following.

5.3.1. Hybrid Hardware Rendering and Ray-Tracing

Udeshi and Hansen⁶¹ propose a system where OpenGL hardware is used to render the direct illumination on diffuse surfaces including shadows (a shadow volume algorithm^{62, 50} is

used for this purpose). Furthermore, one-bounce indirect illumination for diffuse surfaces is computed on the fly with a hemicube-style approach⁶³ for which the graphics hardware is also used.

Finally, the hardware renders an item buffer that is used to spawn primary rays for all surfaces that are not diffuse. A parallel ray-tracer working on several CPUs of a shared memory system is then used to fill in these non-diffuse parts. Frame rates of several frames per second are achieved with this method, where the rendering of the polygons generated for the shadow volume dominates the rendering times. Replacing the shadow volume method with a shadow map algorithm^{49, 13} could probably remove this bottleneck.

5.3.2. Corrective Texture Mapping

Stamminger et al.⁶⁴ have recently proposed a texture based approach for hybrid ray-tracing and hardware rendering. A scene is first rendered by means of graphics hardware. This rendering can include global illumination effects, e.g. shadows. Although this approximate rendering contains all geometric features of the scene (which is important for navigation), it will in general not cover the whole range of lighting effects, as for example multiple reflections and refractions, or complex reflection characteristics.

In order to improve the quality of these interactive renderings, high-quality samples are acquired asynchronously by ray-tracing. The resulting error values, that is, the differences between these samples and the interactive solution, are stored in *corrective textures* which are mapped onto the corresponding object during the interactive display process. Figure 10 shows the result of the method along with one corrective texture.

As new samples for one specific object are ray-traced, they are splatted into the corrective texture. The area influenced by this new sample depends on the age of the samples already in the texture, as well as on the difference in viewing direction, under which the sample has been generated. Furthermore, the error between the ray-traced sample and the OpenGL rendering is used to guide the placement of new sample rays, so that highly specular regions are updated more frequently than mostly diffuse ones, and dynamic parts of the scene more frequently than static ones.

5.4. Discussion

We have seen that interactive rendering algorithms for generating global illumination solutions on the fly can be grouped into three categories. Hardware-based methods can account only for limited kinds of light paths, and new methods have to be developed for every new effect that is to be simulated. On the other hand, some of these techniques are fast enough to be actually used in applications.

Interactive ray-tracing methods are conceptually the most



Figure 11: Left: the object structure of a sample scene. Each red box corresponds to one object that shares one corrective texture. Right: a resulting rendering exhibiting reflections, refractions, and a caustic. Images courtesy of Marc Stamminger.

general algorithms which allow for simulating almost arbitrary optical effects. Unfortunately, the current hardware is not fast enough to achieve both highly interactive frame rates and a high image quality at the same time, except for relatively simple scenes.

The hybrid methods try to balance the load between CPU and dedicated graphics hardware. In doing so, they often achieve higher frame rates than pure ray-tracing approaches, but on the other hand the rendering quality also tends to be lower due to some resampling step that is required at some point during rendering.

6. Conclusion

In this survey we have reviewed the work of many researchers on interactive display of global illumination solutions. We have seen that a significant number of the methods rely on precomputed global illumination solutions stored in a form that at least loosely resembles a light field. This is not too surprising, since the problem of storing directionally dependent illumination on 2D manifolds naturally leads to a 4D data structure of some kind, which can then be interpreted as a light field. Unfortunately, four dimensions are not sufficient to extend the approaches to participating media if the viewer is to be allowed to stand inside the medium. An additional dimension, however, would further amplify the storage problems of these methods.

It is interesting to note that those representations used most frequently in interactive and realtime applications (and especially in games) make further simplifying assumptions and reduce the 4D light field to 2D environment maps. This certainly is related to the tradeoff between storage costs and efficiency of reconstruction for the light field methods, as discussed in Sections 3 and 4. We can expect these disadvantages of light fields to become less important as more research goes into more efficient compression schemes and adaptive acquisition techniques.

Finally, there needs to be more research on methods that

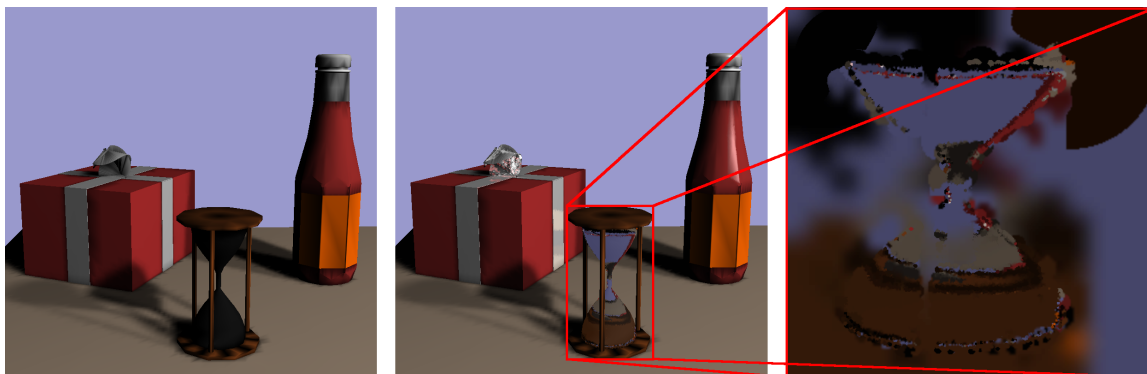


Figure 10: Left: hardware rendering of a scene with diffuse direct illumination only. Center: high-quality solution generated by corrective texture mapping. Right: the corrective texture used for one of the objects. Images courtesy of Marc Stamminger.

can deal with dynamic scenes by recomputing the global illumination on the fly. The work that has been done on interactive ray-tracing and hybrid ray-tracing/hardware rendering is promising, but not feasible for many practical applications at the moment. Since many of these techniques are actually bound by memory bandwidth rather than CPU performance, and the available bandwidth does not grow as quickly as CPU speed, more research is required to overcome this problem.

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