

Applications of Pixel Textures in Visualization and Realistic Image Synthesis

Wolfgang Heidrich, Rüdiger Westermann,
Hans-Peter Seidel, Thomas Ertl

Computer Graphics Group
University of Erlangen
{heidrich,wester,seidel,ertl}@informatik.uni-erlangen.de

Abstract

With fast 3D graphics becoming more and more available even on low end platforms, the focus in developing new graphics hardware is beginning to shift towards higher quality rendering and additional functionality instead of simply higher performance implementations of the traditional graphics pipeline. On this search for improved quality it is important to identify a powerful set of orthogonal features to be implemented in hardware, which can then be flexibly combined to form new algorithms.

Pixel textures are an OpenGL extension by Silicon Graphics that fits into this category. In this paper, we demonstrate the benefits of this extension by presenting several different algorithms exploiting its functionality to achieve high quality, high performance solutions for a variety of different applications from scientific visualization and realistic image synthesis. We conclude that pixel textures are a valuable, powerful feature that should become a standard in future graphics systems.

CR Categories: I.3.3 [Computer Graphics]: Picture/Image Generation—Bitmap and framebuffer operations I.3.3 [Computer Graphics]: Picture/Image Generation—Display algorithms I.3.6 [Computer Graphics]: Methodology and Techniques—Standards I.3.7 [Computer Graphics]: Three-Dimensional Graphics and Realism—Color, Shading, Shadowing and Texture

1 Introduction

Until recently, the major concern in the development of new graphics hardware has been to increase the performance of the traditional rendering pipeline. Today, graphics accelerators with a performance of several million textured, lit triangles per second are within reach even for the low end. As a consequence, we see that the emphasis is beginning to shift away from higher performance towards higher quality and an increased feature set that allows for the use of hardware in a completely new class of graphics algorithms.

Recent examples for this development can be found in version 1.2 of the OpenGL API [17]: both 3-dimensional textures [2, 23],

which can be used for volume rendering, and the imaging subset, a set of extensions useful not only for image-processing, have been added in this version of the specification. Bump mapping and procedural shaders are only two examples for features that are likely to be implemented at some point in the future.

On this search for improved quality it is important to identify a powerful set of orthogonal building blocks to be implemented in hardware, which can then be flexibly combined to form new algorithms. We think that the pixel texture extension by Silicon Graphics [9, 12] is a building block that can be useful for many applications, especially when combined with the imaging subset.

In this paper, we use pixel textures to implement four different algorithms for applications from visualization and realistic image synthesis: fast line integral convolution (Section 3), shadow mapping (Section 4), realistic fog models (Section 5), and finally environment mapping for normal mapped surfaces (Section 6). Not only do these algorithms have a practical use by themselves, but they also demonstrate the general power of pixel textures.

The remainder of this paper is organized as follows. In Section 2 we first describe the functionality added by the pixel texture extension as well as the imaging subset, which we also use for our algorithms. Then, we introduce our algorithms for the above applications in Sections 3-6. Finally, in Section 7, we conclude by discussing some observations we made while using pixel textures.

2 Pixel Textures and the OpenGL 1.2 Imaging Subset

The imaging subset consists of a number of extensions that have been around for some time. It introduces features such as histograms, convolutions, color lookup tables and color matrices. These are standard operations in image processing, but also have applications in many other areas, as we will show below.

Of the many features of this subset, we only use color matrices and color lookup tables. A color matrix is a 4×4 matrix that can be applied to any $RGB\alpha$ pixel group during pixel transfer (that is, while reading images from or writing images to the framebuffer, but also while specifying a new texture image).

In addition, separate color lookup tables for each of the four components can be specified both before and after the color matrix. These allow for non-linear transformations of the color components. Scaling and biasing of the components is also possible at each of these stages. For a detailed discussion of these features and the whole imaging subset, refer to [17].

The pixel texture extension adds an additional stage to this pipeline, which is located after the second color lookup table (see Figure 1). This stage interprets the color components R, G, B, and α as texture coordinates s , t , r , and q , respectively. Pixel textures only apply during the transfer of pixels to and from the framebuffer, but not to the loading of textures.

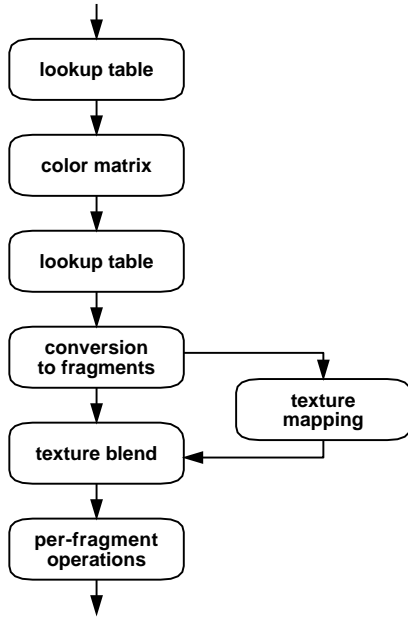


Figure 1: Part of the rendering pipeline including pixel textures and the imaging extension. Only features used in this paper are depicted.

A number of other restrictions apply. The dimensionality of the texture has to match the number of components of the original pixel (that is, before any lookup tables or color matrices are applied). For example, if the original pixel has two components, luminance and alpha, then the texture has to be 2-dimensional. On the other hand, if the format of the original pixels is $RGB\alpha$, then a 4-dimensional texture is required. While 4-dimensional textures are not part of the OpenGL standard, they are also available as an extension from SGI. An additional restriction of the current pixel texture implementation is that 1- and 2-dimensional textures are not directly supported, but can be simulated using degenerated 3-dimensional textures.

It is also important to note that R, G, B, and α are directly used as texture coordinates s , t , r , and q . A division by q does not take place. This means that perspective texturing is not possible with pixel textures.

In a sense, pixel textures provide a limited form of deferred shading [15], in that they allow one to interpolate color coded texture coordinates across polygons. These can be used to evaluate arbitrary functions of up to four variables on a per pixel basis.

3 Line Integral Convolution

Now that we have introduced the basic functionality of pixel textures and the imaging subset, we will demonstrate their effective use in several examples from realistic image synthesis and scientific visualization. We start by introducing a hardware-accelerated method for 2D line integral convolution (LIC), which is a popular technique for generating images and animations from vector data.

LIC was first introduced in [3] as a general method to visualize flow fields and has been further developed to a high degree of sophistication in [22]. The basic idea consists of depicting the directional structure of a vector field by imaging its integral curves or stream lines. The underlying differential equation to be solved for obtaining a path $\sigma(s)$ through an arbitrary point x whose orienta-

tion coincides with the vector field is given by

$$\frac{d}{ds}\sigma(s) = f(\sigma(s)). \quad (1)$$

By solving Equation 1 with the initial condition $\sigma(0) = x$, the stream line of a particle starting at position x thereby undergoing the interior forces of the vector field can be computed.

In order to show the directional structure of the vector field, the intensity for a pixel located at $x_0 = \sigma(s_0)$ is computed by convolving an input texture T (usually given by a random noise field) with a filter kernel k along the stream line:

$$I(x_0) = \int_{s_0-L}^{s_0+L} k(s-s_0)T(\sigma(s))ds \quad (2)$$

Thus, along the stream curves the pixel intensities are highly correlated, whereas they are independent (see Figure 2) in the perpendicular direction.

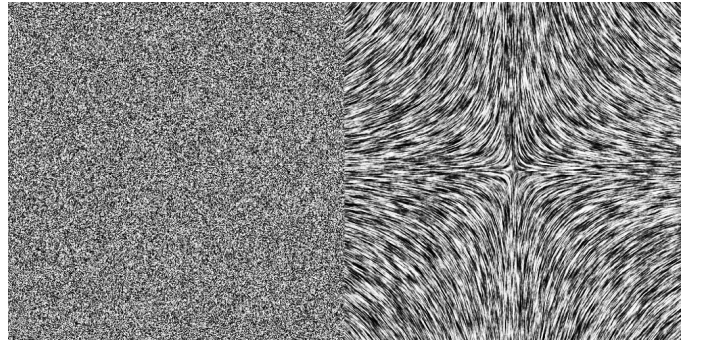


Figure 2: The random noise input texture and the LIC image after 20 iteration steps.

The performance of LIC-algorithms depends on the methods used to update particle positions, and to perform the integral convolution. To solve Equation 2 numerically the input texture is sampled at evenly spaced points along the curves. These points are interpolated from the vector field which is usually given at discrete locations on a uniform grid. Although higher-order interpolation schemes have been exploited to obtain accurate curves, we only use bilinear interpolation for the update of particle positions. This leads to less accurate results but it allows us to compute pixel intensities in real-time, which is of particular interest for previewing purposes and animations.

In order to exploit pixel textures for line integral convolution the following textures are generated: The noise values are stored in a luminance-texture (T) and the 2-dimensional vector field is stored in the RG color components of a RGB -texture. Since texture values are internally clamped to $[0 \dots 1]$ the vector field is split into its positive ($V+$) and negative ($V-$) parts. Their absolute values are stored in two separate textures. Negative vectors can then be simulated by mapping the negative parts but with a subtractive blending model.

Figure 3 outlines the texture based algorithm to compute LIC images. Each pixel of the image is initialized with a color representing the location of that pixel within the vector field. This is accomplished by drawing a quadrilateral that exactly covers the domain with appropriately specified vertex colors. In each integration step the integrand in Equation 2 is evaluated by reading the pixel values from the framebuffer and writing them back in an additional buffer with enabled pixel texture T . The result is copied into the accumulation buffer thereby accounting for the scale factor k . The update of pixel positions is performed in two passes. First, pixel

Each pixel now stores the information necessary to re-project into world space coordinates with respect to the present viewing definition. From there, the projection into the light source space allows us to obtain the entry in the shadow map whose value has to be compared for each pixel.

Since the projective matrices $M_{UnProjView} = M_{ProjView}^{-1}$ and $M_{ProjLight}$ are known, it suffices to build a single matrix $CM_{All} = M_{ProjLight} \cdot M_{UnProjView}$ which accomplishes the transformation. It is loaded on top of the color matrix stack, but it has to be slightly modified to ensure that the transformed Z'_{light} values are also stored in the α -channel. This allows us to take advantage of the α -test later on.

We copy the framebuffer once to apply the color matrix multiplication:

$$\begin{bmatrix} X'_s \\ Y'_s \\ Z'_{light} \\ Z'_{light} \end{bmatrix} = CM_{All} \cdot \begin{bmatrix} X_s \\ Y_s \\ Z_{view} \\ Z_{view} \end{bmatrix}$$

As a result, in each pixel the RG color components specify the entry in the shadow map, whereas the B α components contain the z-value with respect to the light source.

Finally, the framebuffer is read and written once more, thereby texturing pixel values with the pre-computed shadow map. By choosing the blending function appropriately the texture values are subtracted from those already in the framebuffer and clamped to $[0 \dots 1]$:

$$\begin{bmatrix} X'_s \\ Y'_s \\ Z'_{light} \\ Z'_{light} \end{bmatrix} - \begin{bmatrix} 1 \\ 1 \\ 1 \\ Z_{light} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ Z_{diff} \end{bmatrix}.$$

Only where the object is in shadow the generated pixel values have α -values larger than zero.

All pixels are now copied onto each other. However, by exploiting the OpenGL α -test, those pixels where $\alpha \neq 0$ will be rejected. All pixels which are drawn are biased with (1,1,1,0) using the OpenGL imaging subset. In this way the result can be directly used as a shadow mask for the rendered scene on a per-pixel basis.

Due to the lack of projective pixel textures, this shadow-map algorithm is currently restricted to orthographic views and parallel light sources. Nonetheless, it can be very useful, for example in volume rendering applications. For other applications, an additional pixel texture mode that provides the perspective division would allow for point lights and perspective views.

5 Complex Fog Models

The next application we are going to look at is fog. In flight simulators and other outdoor sceneries, fog can significantly contribute to the realism of a scene.

Most graphics boards offer two kinds of fog simulation: the simpler version computes the absorption using a linear color ramp that depends on the z -coordinate of a point in eye space, and the second, more expensive version computes an exponential decay along the z -direction. The color of a pixel is then chosen as

$$C_p := (1 - \text{absorption}) \cdot C_f + \text{absorption} \cdot C_o, \quad (3)$$

where C_o is color of the object, and C_f is a global fog color, which is used to fake emission and scattering effects.

It is well known [14, 5] that the intensity of a point in a participating media should decay exponentially with the distance d from the point of view:

$$\text{absorption} = e^{-\int_0^d \sigma(t) dt}. \quad (4)$$

For a homogeneous medium, that is, for a constant fog density σ throughout space, this equation simplifies to

$$\text{absorption} = e^{-d \cdot \sigma}.$$

Of course, a linear ramp is only a very crude approximation of this function, but even the exponential version of hardware fog approximates the distance of a point from the eye by the point's z -coordinate.

5.1 Euclidean Distance Fog

This exponential version does produce more realistic images, but is still insufficient for several applications, since the distance (and hence the obstruction by fog) is underestimated for objects on the periphery of the image (see Figure 5). As a consequence, the brightness of objects changes with the viewing direction, even if the eye point remains the same. This results in seams when multiple images of the scene are warped together to form a composite image, for example for large projection screens.

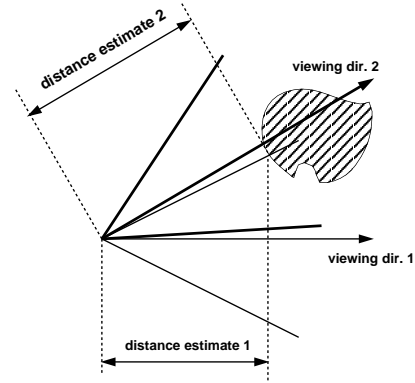


Figure 5: Simple fog systems that use the z -coordinate as an estimate for the distance of a point from the eye underestimate the distance in particular for points on the periphery of the image. Moreover, the distance estimate changes with the viewing direction.

In the following we introduce an algorithm that computes fog based on the true Euclidean distance of a point from the eye. This Euclidean distance is computed via lookup tables and the color matrix, and finally an exponential fog function is applied through the use of pixel textures. The method requires two passes in which the geometry is rendered, one framebuffer read, and one framebuffer write with pixel textures.

As a first step, the scene is rendered with the world coordinates x_w, y_w , and z_w being assigned as colors to each vertex. These coordinates have to be normalized to the range $[0 \dots 1]$ through a linear function. Similar linear mappings are required in several of the following steps, but will be omitted in this discussion for reasons of simplicity.

Then, a color matrix containing the viewing transformation is specified, a color lookup table containing the function $f(x) = x^2$ is activated, and the framebuffer is read to main memory. At this point we have an image containing x_e^2, y_e^2 , and z_e^2 , the squares of each point's coordinates in eye space, as a RGB color.

We write this image back to the framebuffer after loading a color matrix that assigns the sum of R, G, and B to the red component and specifying a color table that takes the square root. Now the Euclidean distance of each point is coded into the red component. Consequently, it can be used to reference into a pixel texture containing Equation 4. This 1-dimensional texture has to be specified

as a degenerate 3-dimensional texture, since the initial format of the image is RGB.

After this step, the framebuffer contains the absorption factor from Equation 4 for each pixel. Finally, the scene is rendered again, this time with its regular textures and lighting, but blending is set up in such a way, that these colors are blended with the current framebuffer content according to Equation 3.

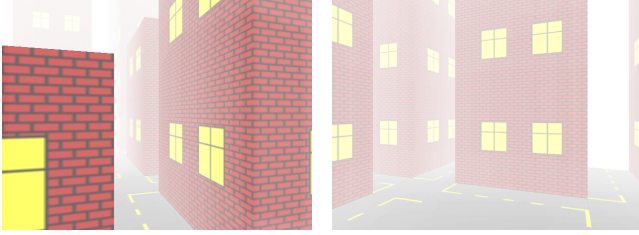


Figure 6: Two examples for Euclidean distance fog.

Figure 6 shows images rendered with this method on a SGI Octane MXI. This scene can be rendered at 15 frames/sec. for a 640×480 resolution.

5.2 Layered Fog

Both the traditional hardware fog and the algorithm presented above have in common that the fog is uniform, that is, its density is constant for the whole scene. Layered fog is a concept that softens this restriction, by allowing the density to change as a function of height [13]. This means that a visual simulation application could specify a relatively dense layer of fog on the ground, followed by an area of relatively clear sky, and then a layer of clouds higher up.

The algorithm for layered fog that we present in the following is similar to the Euclidean distance fog algorithm presented above. However, instead of a 1-dimensional pixel texture we now have to use a 2-dimensional or 3-dimensional one. The idea of fog computation through table lookups is borrowed from [13], but our method is faster due to the use of pixel textures, which allows us to perform all computations in hardware.

Due to the restriction to layers of constant fog density, the exponent from Equation 4 simplifies to

$$\int_0^d \sigma(t) dt = \frac{d}{|y_w - y_{e,w}|} \int_{y_{e,w}}^{y_w} \sigma(y) dy, \quad (5)$$

where $y_{e,w}$ is the y-coordinate of the eye point in world space, y_w is an object point in world coordinates, and d is the Euclidean distance between the two points as above.

This is merely a scaling of the absorption for a vertical ray from an object point at height y_w to an eye point at height $y_{e,w}$ (also see Figure 7).

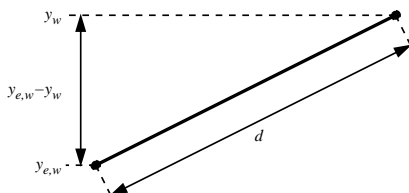


Figure 7: For layered fog, the absorption along an arbitrary ray can be computed directly from the absorption for a vertical ray.

An interesting observation is that Equation 5 (and thus Equation 4) is only a function of 3 variables: $y_{e,w}$, y_w and d . The latter two of these vary per pixel, whereas the first one is a constant within each frame. We propose two slightly different methods for implementing layered fog, both are modifications of the algorithm presented in Section 5.1.

The first method uses a 3-dimensional texture that directly codes $e^{-d/(|y_w - y_{e,w}|) \int_{y_{e,w}}^{y_w} \sigma(y) dy}$. To compute the three texture coordinates, we read the framebuffer to main memory as in Section 5.1, but this time with a color matrix and lookup tables that store x_e^2 , y_e^2 , z_e^2 and y_w as an RGB α image in main memory. During the writing phase, the color matrix and lookup tables are set up so that they store d and y_w in the R and G components. Biasing the blue component by the global constant $y_{e,w}$ yields the third color component, and thus the third texture coordinate for the pixel texture. Since the intermediate format of the image is RGB α , the 3-dimensional fog texture has to be stored as a degenerate 4-dimensional pixel texture.

Instead of the biasing step, it is also possible to only use d and y_w to effectively reference a 2-dimensional texture, which then has to change every time the eye point moves vertically. This has the advantage that smaller texture RAM sizes are sufficient, but the disadvantage that new textures have to be downloaded to texture RAM if the height of the eye changes.

Figure 8 shows images rendered with layered fog, again on a SGI Octane MXI. With both algorithms, this scene can be rendered at 12 frames/sec. for a 640×480 image resolution. This time is marginally larger than the time for Euclidean distance fog presented above, due to the use of RGB α instead of RGB images.

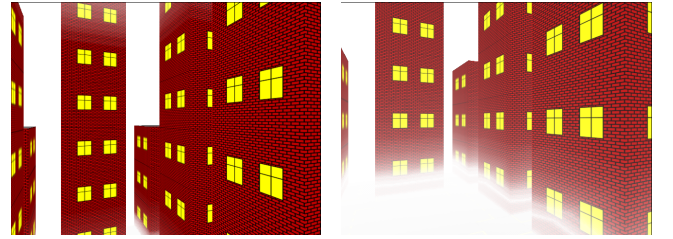


Figure 8: Two examples for layered fog with a dense layer of ground fog and a layer of clouds on the top.

Both Euclidean distance and layered fog are most useful in visual simulation applications where realism is a top requirement. They allow for a more accurate simulation of visibility in certain situations. The standard hardware fog which improves the vision in peripheral regions is not adequate in these situations. The methods presented here allow for an efficient, hardware based implementation of both layered and Euclidean distance fog.

6 Environment Mapping for Normal-Mapped Surfaces

As a final example for applications of pixel textures, we discuss an algorithm for applying spherical environment maps [8] to surfaces with normal maps. Instead of the spherical parameterization we describe here, it is also possible to use view-independent parabolic maps [11, 10].

We use the term “normal map” for textures containing color coded normals for each pixel in object space. Normal maps have the advantage that the expensive operations (computing the local surface normal by transforming the bump into the local coordinate frame) have already been performed in a preprocessing stage. All that remains to be done is to use the precomputed normals for lighting each pixel. As we will show in the following, this allows us to

use a fairly standard rendering pipeline, which does not explicitly support bump mapping. Another advantage of normal maps is that recently methods have shown up for measuring them directly [20], or for generating them as a by-product of mesh simplification [4].

The parameterization used most commonly in computer graphics hardware today, is the *spherical parameterization* for environment maps [8]. It is based on the simple analogy of a small, perfectly mirroring ball centered around the object. The image that an orthographic camera sees when looking at this ball from a certain viewing direction is the environment map.

With this parameterization, the reflection of a mirroring object can be looked up using the following calculations (see Figure 9 for the geometry). For each vertex compute the reflection vector \mathbf{r} of the per-vertex viewing direction \mathbf{v} . A spherical environment map which has been generated for an orthographic camera pointing into direction \mathbf{v}_0 , stores the corresponding radiance information for this direction at the point where the reflective sphere has the normal $\mathbf{h} := (\mathbf{v}_0 + \mathbf{r}) / \|\mathbf{v}_0 + \mathbf{r}\|$. If \mathbf{v}_0 is the negative z -axis in viewing coordinates, then the 2D texture coordinates are simply the x and y components of the normalized halfway vector \mathbf{h} . For environment mapping on a per-vertex basis, these texture coordinates are automatically computed by the texture coordinate generation mechanism of OpenGL.

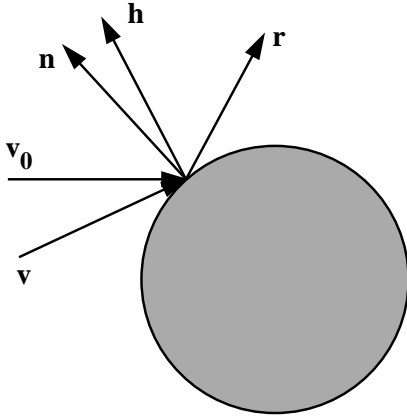


Figure 9: The lookup process in a spherical environment map.

An interesting observation is that for orthographic cameras, the viewing direction \mathbf{v} is identical to the reference viewing direction \mathbf{v}_0 for all vertices, and thus, the halfway vector \mathbf{h} is identical to the surface normal \mathbf{n} . This approximation does not work well for smooth, planar objects, as it causes these objects to receive a single, solid color. However, the approximation can be used for bump-mapping algorithms, since these typically introduce a lot of high-frequency detail, so that the artifacts are rarely noticeable.

This means, that the information from a normal map can be directly used to look up a mirror reflection term in a spherical environment map. The algorithm to do this uses pixel textures, and works as follows: First, the object is rendered with the normal map as a texture, and all rendered pixels are marked in the stencil buffer. The resulting image is read back to main memory. During this operation, a color matrix can be used to map the normals from object space into eye space, where the environment map is specified. This yields an image containing eye space normals for each visible pixel.

A second rendering pass, in which the 2-dimensional environment map is applied as a degenerate 3-dimensional texture, is then employed to look up the mirror reflection for each pixel (only pixels previously marked in the stencil buffer are considered). Figure 10 shows some images that have been generated with this technique.

In addition to the mirror term, it is also possible to add local



Figure 10: Examples for normal-mapped surfaces with applied environment maps. In the top row, only the mirror components are shown. For the bottom row, Phong lighting has been added with techniques described in [10].

Phong illumination using additional rendering passes. These algorithms require operations from the imaging subset but no pixel textures, and are therefore not described here. They are discussed in detail in [10].

Spherical environment maps are widely used in interactive computer graphics, but they have the disadvantage that they need to be regenerated for every new viewing position and -direction. In [11], a different, parabolic parameterization has been introduced, which does not have this disadvantage. Since this parameterization also uses the halfway vector \mathbf{h} for the environment lookup, the same technique can be applied to these maps. A combination of parabolic environment maps and pixel textures with support for projective texturing allows one to apply *one* environment map to a normal mapped surface for *all* viewing positions and -directions (a detailed discussion of this topic can be found in [10]. Without projective texturing, parabolic environment maps can, like spherical maps, only be used for one viewing direction.

The techniques discussed in this section provide efficient ways for applying environment maps to normal mapped surfaces. Combined with techniques for local illumination, described in [11], this allows for the efficient implementation of normal mapped surfaces.

7 Discussion

In this paper we have used the SGI pixel texture extension in a number of algorithms for a variety of different applications: hardware-based line-integral convolution, shadow mapping, complex fog models and environment mapping for normal mapped surfaces.

These algorithms provide efficient, high quality implementations for problems in visualization and realistic image synthesis. In addition to being valuable contributions on their own, they also demonstrate some techniques for using pixel textures and the new OpenGL imaging subset. In the following, we will discuss some observations we have made while working on these algorithms.

Firstly, the OpenGL imaging subset is also useful for many applications outside traditional image processing. Especially when combined with pixel textures, the color matrix is a powerful way for transforming points and vectors between different coordinate systems. Lookup tables and scaling/biasing additionally allow for non-linear operations such as the computation of a Euclidean distance.

Secondly, we should mention the major limitation of pixel textures in the presented scenarios. The most crucial drawback stems from the limited depth of the available frame buffers. When data is stored in a pixel texture and rendered into the framebuffer usually precision is lost. For example, if the shadow map in which z-values are stored is mapped and drawn into an 8 Bit display, quantization artifacts arise which can be seen particularly at shadow boundaries. The same holds for the simulation of realistic fog models where the exponential attenuation is quantized into a limited number of bins. Furthermore, the frame buffer depth strongly determines the size of textures that can be accessed. Effectively, only textures up to 256x256 can be mapped using 8 Bit displays.

In our applications we therefore used the deeper visuals provided by the Octane graphics system. With 12 bits per component, these quantization artifacts are already softened significantly. Nonetheless for some applications such as shadow maps, even deeper visuals would be beneficial. As a consequence, we see specifically designed visuals or additional buffers with limited functionality but higher precision as one of the dominant features in future generation graphics hardware.

As a final observation, we found that the flexibility of the pixel texture extension could be further improved through two minor changes in the specification. One change regards the support of projective textures. By introducing a mode that performs a perspective division by the q component, this important feature could be supported. This would, for example, open the door for a general shadow map algorithm as shown in Section 4 and view-independent environment maps (Section 6), but other applications are also possible. Of course it could be argued that a perspective divide for every pixel is an expensive operation, but on the other hand there are applications, such as shadow mapping, where this operation has to be performed at some point. It is then better to have hardware support for this instead of forcing the user to fall back to software.

The second change regards the coupling of image format and dimensionality of the pixel texture. We think that there really is no good reason for this. In many of the methods we have demonstrated how the number of color components can be expanded or reduced through the use of color matrices and lookup tables. Therefore it is reasonable to allow pixel textures with an arbitrary dimension to be used with images of any internal format.

While these two changes would certainly help to make the pixel texture extension even more powerful, even the current specification has many applications. The described algorithms only show a small part of these applications of pixel textures, but they demonstrate the potential of the extension is for achieving high quality, high performance renderings. We believe that pixel textures should become a standard component of the graphics pipeline, and that this extension should become part of the OpenGL standard.

8 Acknowledgments

We would like to thank Peter-Pike Sloan for a discussion of the shadow map algorithm, and the anonymous reviewers for their valuable comments.

References

- [1] Kurt Akeley. RealityEngine graphics. In *Computer Graphics (SIGGRAPH '93 Proceedings)*, pages 109–116, August 1993.
- [2] Brian Cabral, Nancy Cam, and Jim Foran. Accelerated volume rendering and tomographic reconstruction using texture mapping hardware. In *1994 Symposium on Volume Visualization*, pages 91–98, October 1994.
- [3] Brian Cabral and Leith Casey Leedom. Imaging vector fields using line integral convolution. In *Computer Graphics (SIGGRAPH '93 Proceedings)*, pages 263–272, August 1993.
- [4] Jonathan Cohen, Marc Olano, and Dinesh Manocha. Appearance-preserving simplification. In *Computer Graphics (SIGGRAPH '98 Proceedings)*, pages 115–122, July 1998.
- [5] Robert A. Drebin, Loren Carpenter, and Pat Hanrahan. Volume rendering. In *Computer Graphics (SIGGRAPH '88 Proceedings)*, pages 65–74, August 1988.
- [6] David Ebert, Kent Musgrave, Darwyn Peachey, Ken Perlin, and Worley. *Texturing and Modeling: A Procedural Approach*. Academic Press, October 1994. ISBN 0-12-228760-6.
- [7] Paul Haeberli and Kurt Akeley. The accumulation buffer: Hardware support for high-quality rendering. In *Computer Graphics (SIGGRAPH '90 Proceedings)*, pages 309–318, August 1990.
- [8] Paul Haeberli and Mark Segal. Texture mapping as a fundamental drawing primitive. In *Fourth Eurographics Workshop on Rendering*, pages 259–266, June 1993.
- [9] Paul Hansen. Introducing pixel texture. In *Developer News*, pages 23–26. Silicon Graphics Inc., May 1997.
- [10] Wolfgang Heidrich. *High-Quality Shading and Lighting for Hardware-Accelerated Rendering*. PhD thesis, University of Erlangen-Nürnberg, 1999. in preparation.
- [11] Wolfgang Heidrich and Hans-Peter Seidel. View-independent environment maps. In *Eurographics/SIGGRAPH Workshop on Graphics Hardware*, pages 39–45, 1998.
- [12] Silicon Graphics Inc. *Pixel Texture Extension*, December 1996. Specification document, available from <http://www.opengl.org>.
- [13] Justin Legakis. Fast multi-layer fog. In *Siggraph '98 Conference Abstracts and Applications*, page 266, July 1998. Siggraph Technical Sketch.
- [14] Marc Levoy. Volume rendering using the fourier projection-slice theorem. In *Proceedings of Graphics Interface '92*, pages 61–69, May 1992.
- [15] Steven Molnar, John Eyles, and John Poulton. PixelFlow: High-speed rendering using image composition. In *Computer Graphics (SIGGRAPH '92 Proceedings)*, pages 231–240, July 1992.
- [16] Jackie Neider, Tom Davis, and Mason Woo. *OpenGL Programming Guide*. Addison Wesley, 1993.
- [17] OpenGL ARB. *OpenGL Specification, Version 1.2*, 1998.

- [18] Mark Peercy, John Airey, and Brian Cabral. Efficient bump mapping hardware. In *Computer Graphics (SIGGRAPH '97 Proceedings)*, pages 303–306, August 1997.
- [19] Ken Perlin and Eric M. Hoffert. Hypertexture. In *Computer Graphics (SIGGRAPH '89 Proceedings)*, pages 253–262, July 1989.
- [20] Holly Rushmeier, Gabriel Taubin, and André Guézic. Applying shape from lighting variation to bump map capture. In *Rendering Techniques '97 (Proceedings of Eurographics Rendering Workshop)*, pages 35–44, June 1997.
- [21] Mark Segal, Carl Korobkin, Rolf van Widenfelt, Jim Foran, and Paul Haeberli. Fast shadow and lighting effects using texture mapping. In *Computer Graphics (SIGGRAPH '92 Proceedings)*, pages 249–252, July 1992.
- [22] Detlev Stalling and Hans-Christian Hege. Fast and resolution independent line integral convolution. In *SIGGRAPH 95 Conference Proceedings*, pages 249–256, August 1995.
- [23] Rüdiger Westermann and Thomas Ertl. Efficiently using graphics hardware in volume rendering applications. In *Computer Graphics (SIGGRAPH '98 Proceedings)*, pages 169–177, July 1998.
- [24] Lance Williams. Casting curved shadows on curved surfaces. In *Computer Graphics (SIGGRAPH '78 Proceedings)*, pages 270–274, August 1978.

